

CKM matrix elements & Fits



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Introduction: CKM matrix

$$\mathcal{L}_{int} = -\frac{g}{\sqrt{2}} (\overline{u}_L, \overline{c}_L, \overline{t}_L) \gamma^\mu V \begin{pmatrix} d_L \\ s_L \\ b_L \end{pmatrix} W_\mu + c.c.$$

quark mixing matrix
(CKM matrix)

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

unitarity + adjustment of relative phase

3 Euler angles + 1 phase

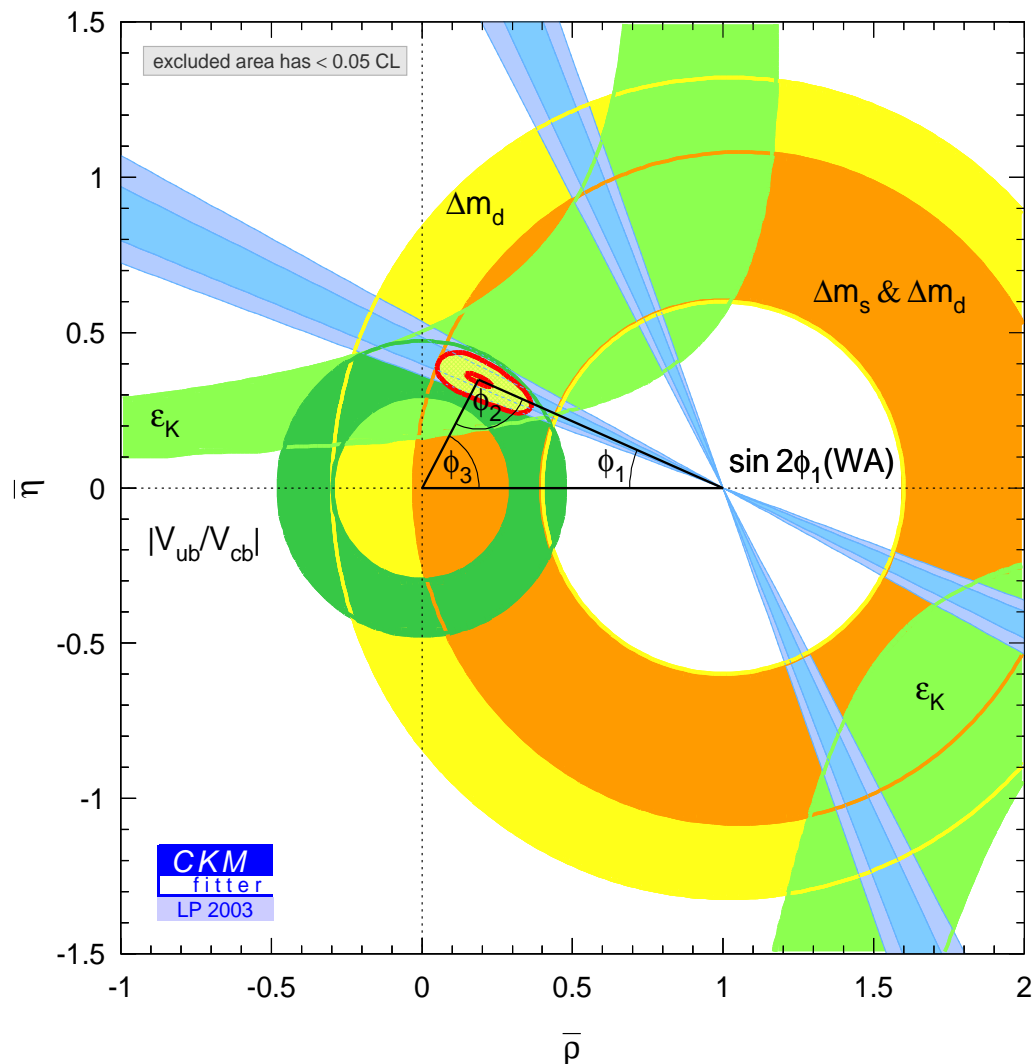
Wolfenstein parametrization: 4 parameters (λ, A, ρ, η)

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - (\lambda^2/2) & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & (1 - \lambda^2/2)A\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

$\rho, \eta \rightarrow$ not measured well
one of the subject in B-factories

Introduction: Unitarity Triangle and Constraints

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0 \quad (\text{unitarity})$$



$|V_{ub}/V_{cb}|$ from semileptonic B-decay:
 → Insensitive to the new physics processes,
 i.e. one of the stable constraints

↑
Essential for the new physics search

Precise measurement on $|V_{ub}|$ & $|V_{cb}|$
 → essential for keeping them as the "constraint"
 e.g. $\sin 2\phi_1$ is getting better and better accuracy

This talk include the status of $|V_{cb}|$ & $|V_{ub}|$ measurements

|V_{cb}| measurements

- 1. Exclusive analyses**
- 2. Inclusive analyses**

|V_{cb}| exclusive analysis: B → D* l ν

Differential decay rate:

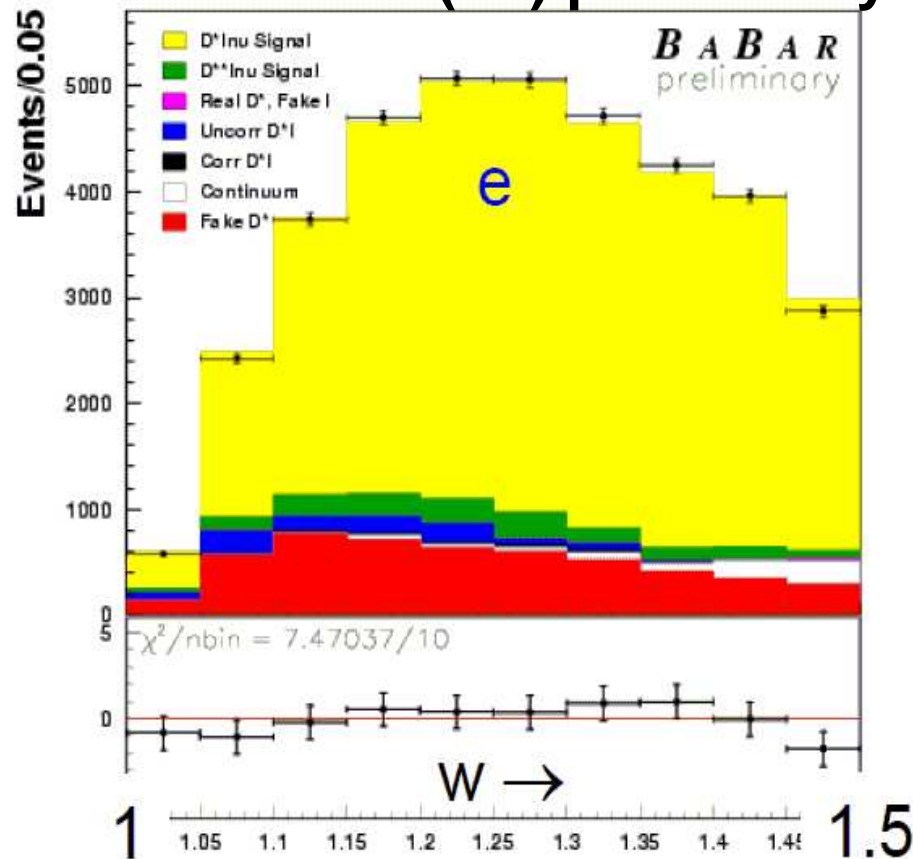
$$\frac{d\Gamma(B \rightarrow D^* l \bar{\nu})}{dw} \propto |V_{cb}^2| F(w)^2$$

$$w = \frac{M_B^2 + M_{D^*}^2 - q^2}{2M_B M_{D^*}}$$

fit w and extract differential decay rate @zero recoil (w=1)

F(1): from HQET

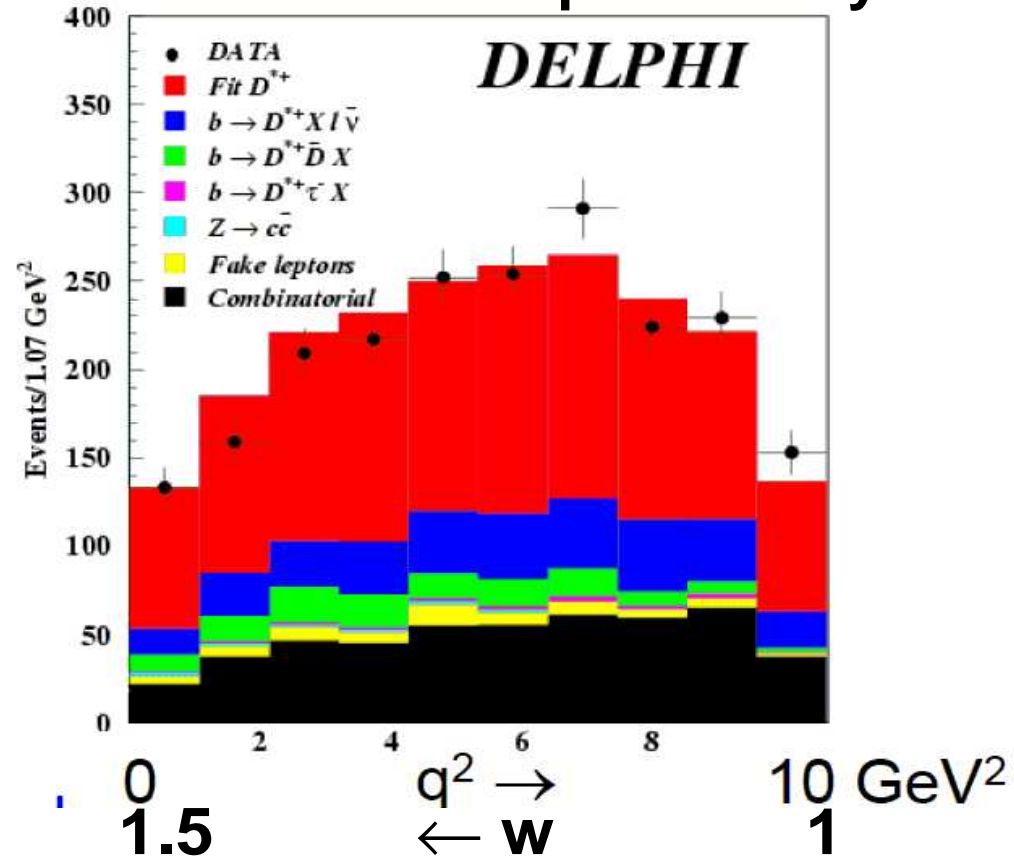
BaBar 86M Υ(4S) preliminary



$$|V_{cb}| F(1) = (34.0 \pm 0.2 \pm 1.3) \times 10^{-3}$$

$$\rho_{A1}^2 = 1.23 \pm 0.02 \pm 0.28$$

DELPHI 3.4 M Z preliminary



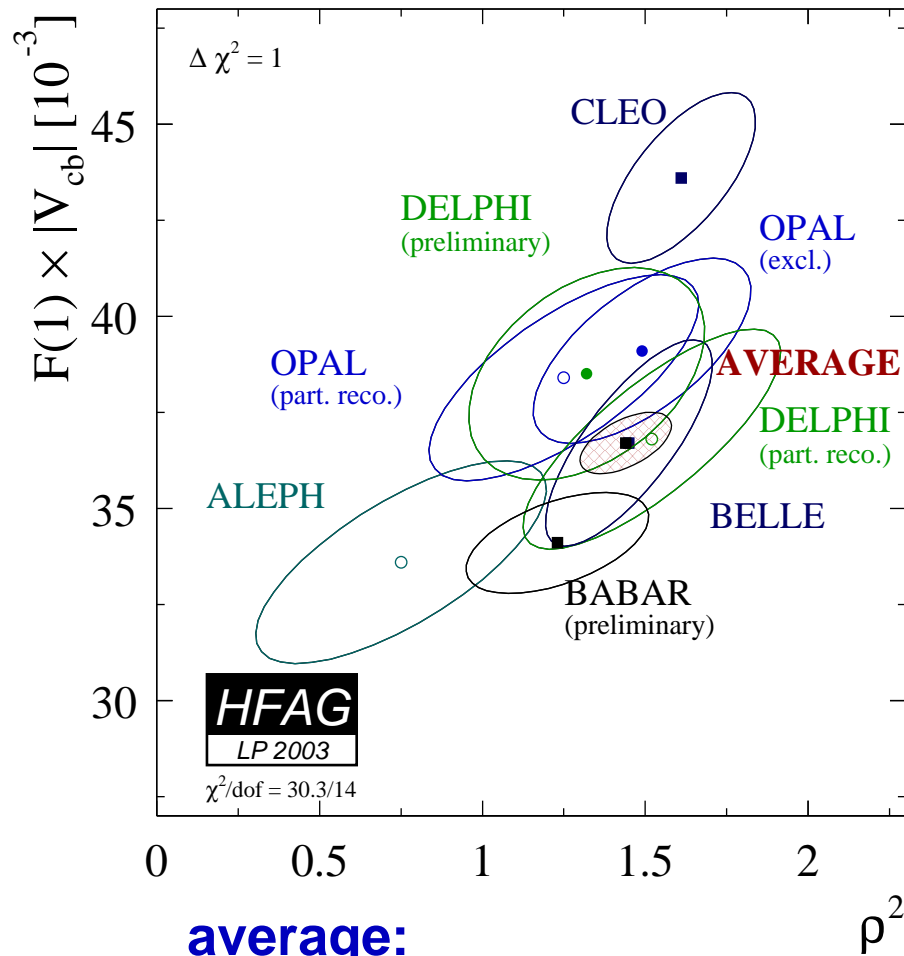
$$|V_{cb}| F(1) = (39.2 \pm 1.8 \pm 2.2) \times 10^{-3}$$

$$\rho_{A1}^2 = 1.32 \pm 0.15 \pm 0.33$$

$|V_{cb}|$ exclusive analysis: Summary

$B \rightarrow D^* l \nu$ (includes BaBar & DELPHI)

$B \rightarrow D l \nu$ (no updates since 2002)



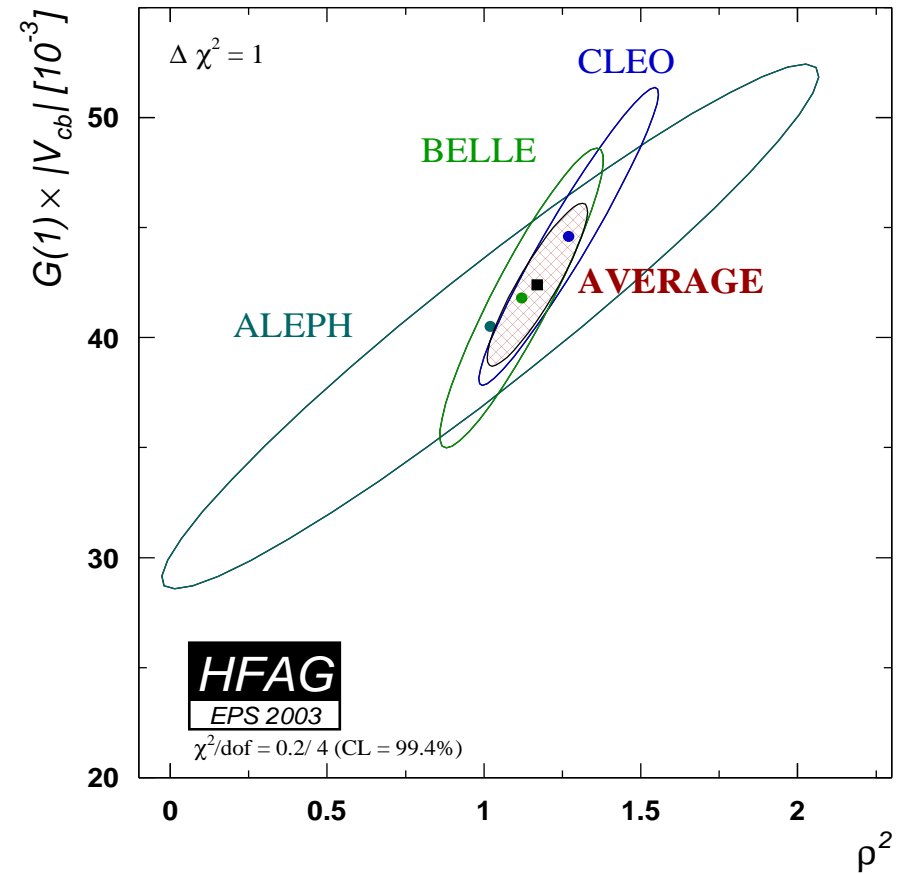
average:

$$|V_{cb}| F(1) = (36.7 \pm 0.8) \times 10^{-3}$$

Using:

$$F(1) = 0.91 \pm 0.04$$

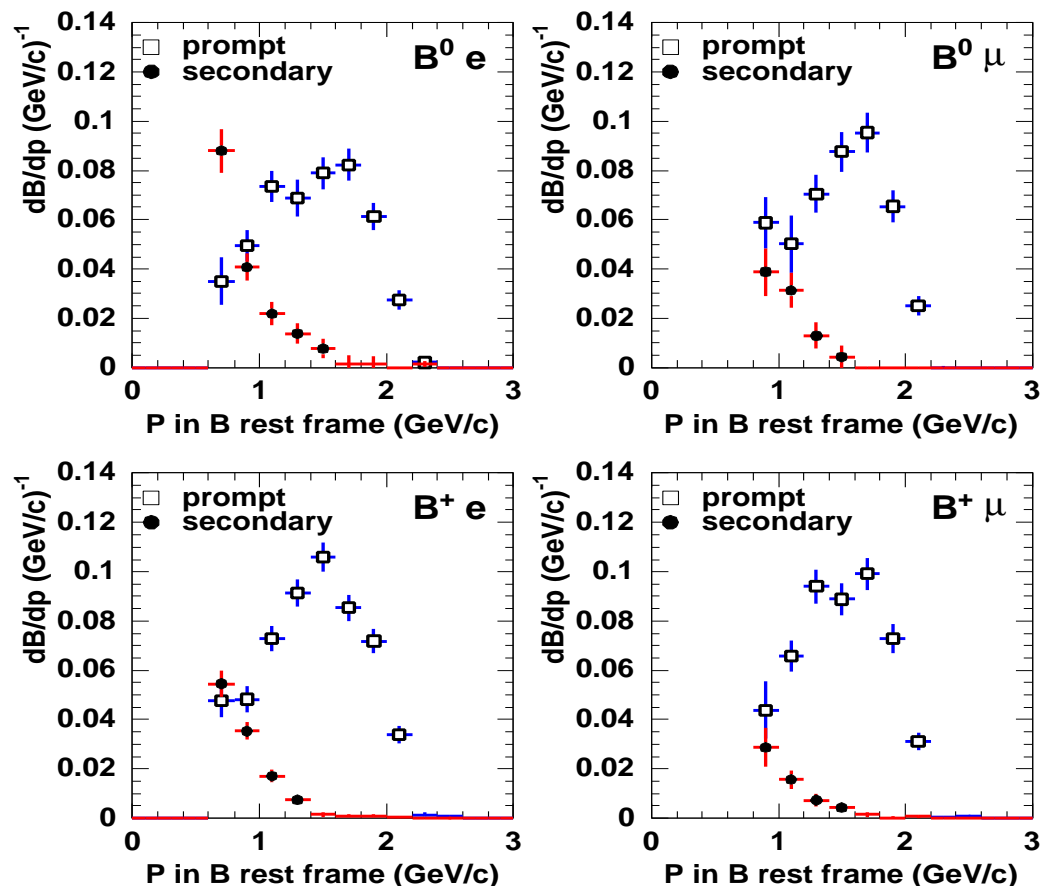
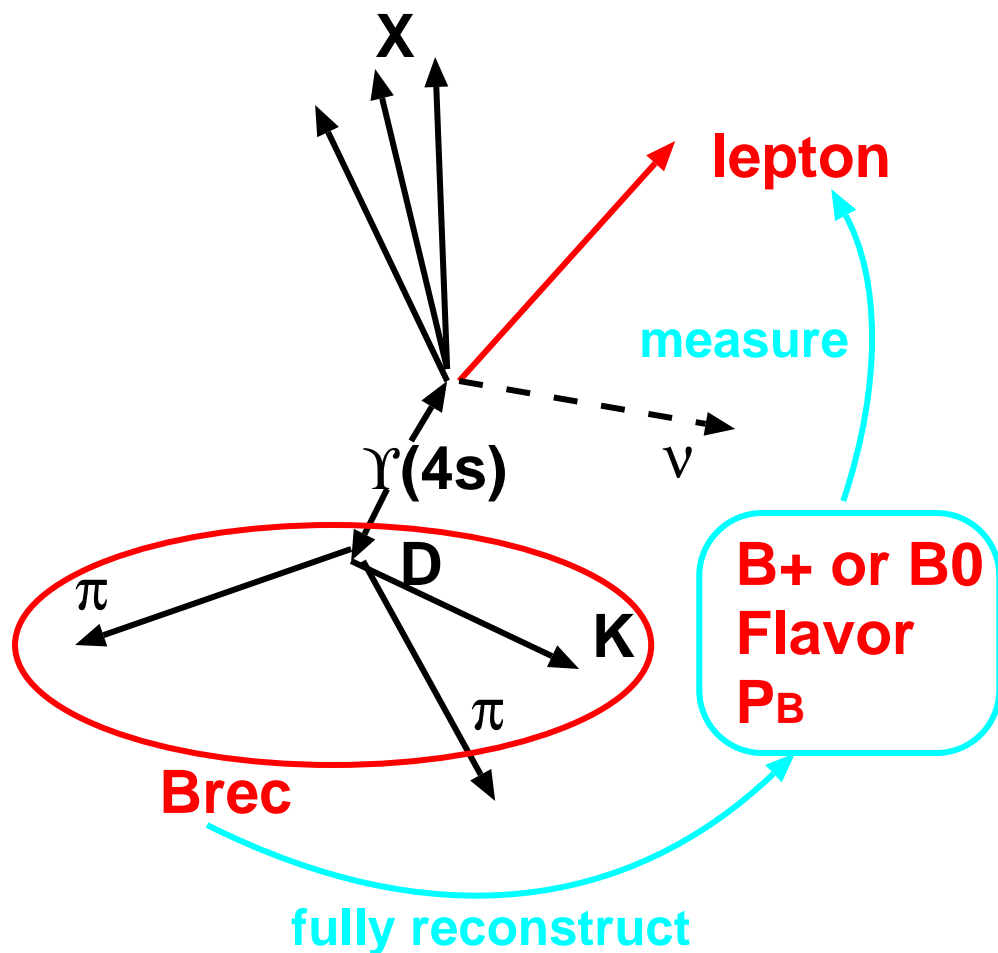
$$|V_{cb}| = (40.2 \pm 0.9 \pm 1.8) \times 10^{-3}$$



$$|V_{cb}| G(1) = (42.1 \pm 3.7) \times 10^{-3}$$

$|V_{cb}|$ inclusive analysis: Lepton momentum spectrum

Lepton spectrum with full reconstruction tag (Belle 78/fb preliminary)



$$\mathcal{B}(B^0 \rightarrow X l \nu) = 10.32 \pm 0.32 \pm 0.29\%$$

$$\mathcal{B}(B^+ \rightarrow X l \nu) = 11.92 \pm 0.26 \pm 0.32\%$$

$$\mathcal{B}(B \rightarrow X l \nu) = 11.19 \pm 0.20 \pm 0.31\%$$

|Vcb| inclusive analysis: moment analyses

Extraction of |Vcb| → HQET/OPE framework

$$\frac{d\Gamma}{dE_l dm_X^2 dq^2} = f(E_l, m_X, q^2, |V_{cb}|, \bar{\Lambda}, \lambda_1, \dots) \quad \bar{\Lambda}, \lambda_1, \dots: \text{nonperturbative quantities}$$

Moments:

$$M_{000} = \int \int \int f dE_l dm_X^2 dq^2, \quad M_{n00} = \int \int \int E_l^n f dE_l dm_X^2 dq^2, \quad M_{0n0} = \int \int \int m_X^{2n} f dE_l dm_X^2 dq^2$$

- constrain $\bar{\Lambda}, \lambda_1$ by measuring various moments: e.g. $\langle E_l \rangle = M_{100}/M_{000} \dots$
- reduce the theoretical uncertainty in |Vcb|, |Vub|

DELPHI 2002,2003:

Mi00, M0i0 (i=1,2,3)

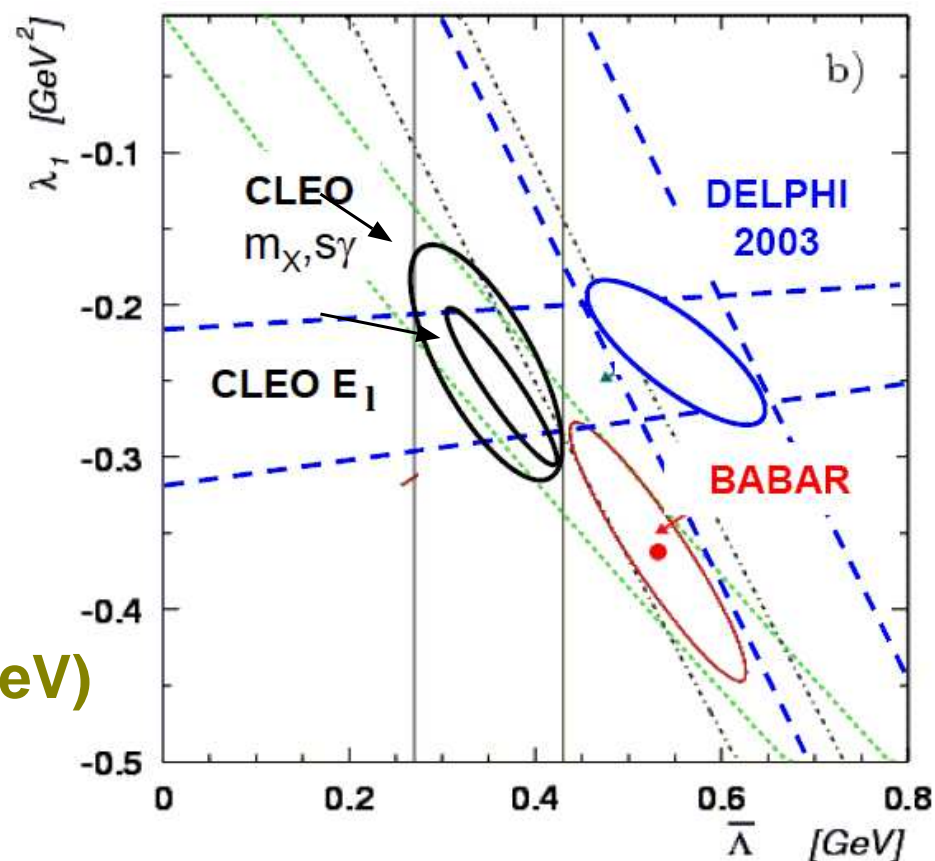
BaBar 2003:

M100 with $E_l > 0.9, \dots, 1.6 \text{ GeV}$

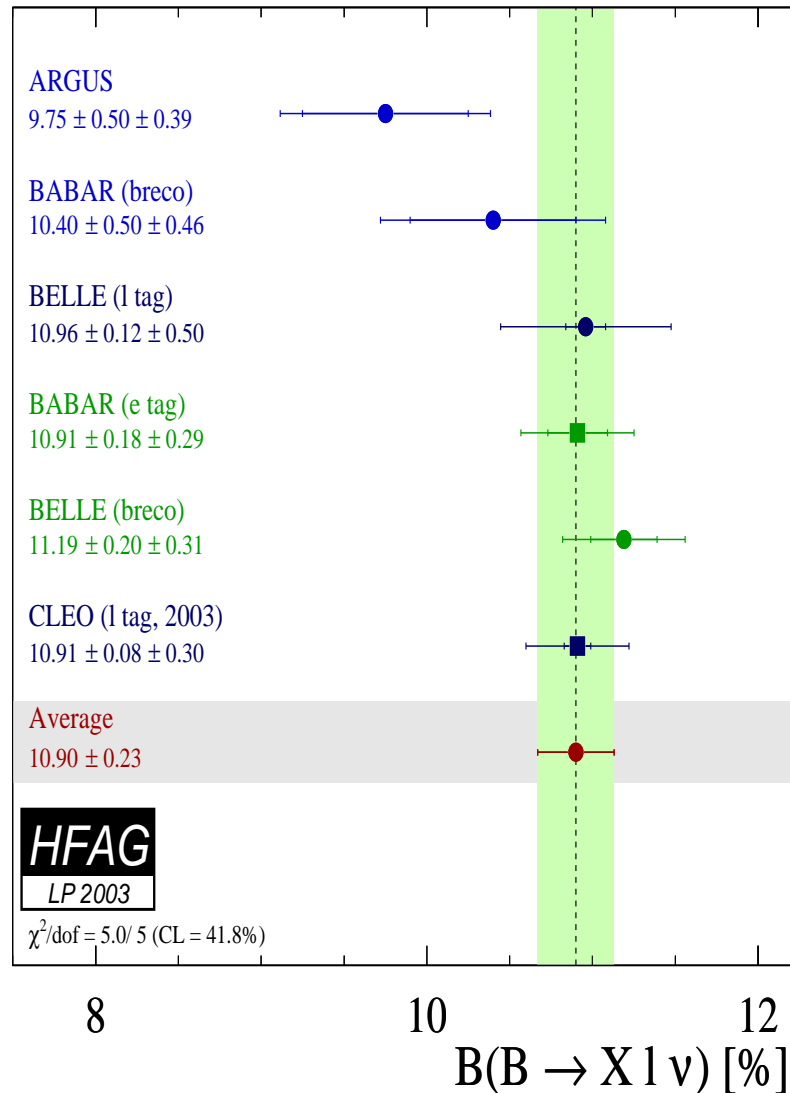
CLEO 2001,2003:

M010 & E_γ moment in $b \rightarrow s\gamma$

M100 & $M_{000}(E_l > 1.5 \text{ GeV}) / M_{000}(E_l > 1.7 \text{ GeV})$



$|V_{cb}|$ inclusive analysis: summary



$$\text{Br}(B \rightarrow X l \nu) = 10.90 \pm 0.23 \%$$

Substantial efforts on reducing the theoretical uncertainty
i.e. extraction of $\bar{\Lambda}$ & λ_1
← moment analyses

For averaging of the $|V_{cb}|$, need:
1. averaged value of $\bar{\Lambda}$ and λ_1 or
2. simultaneous extraction of $\bar{\Lambda}$, λ_1 and $|V_{cb}|$

|Vub| measurements

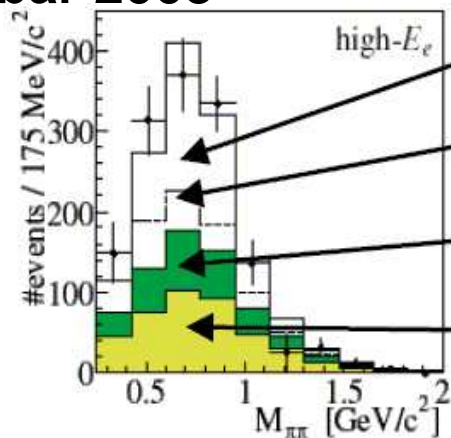
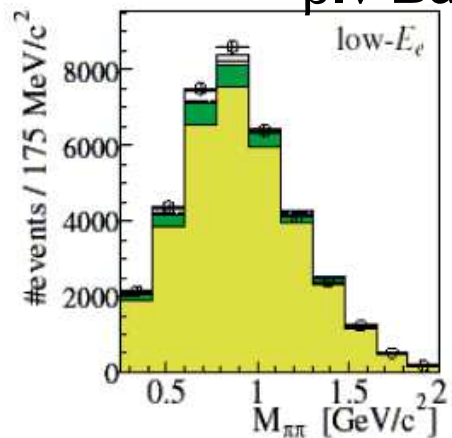
- 1. Exclusive analyses**
- 2. Inclusive analyses**

$|V_{ub}|$ exclusive analyses

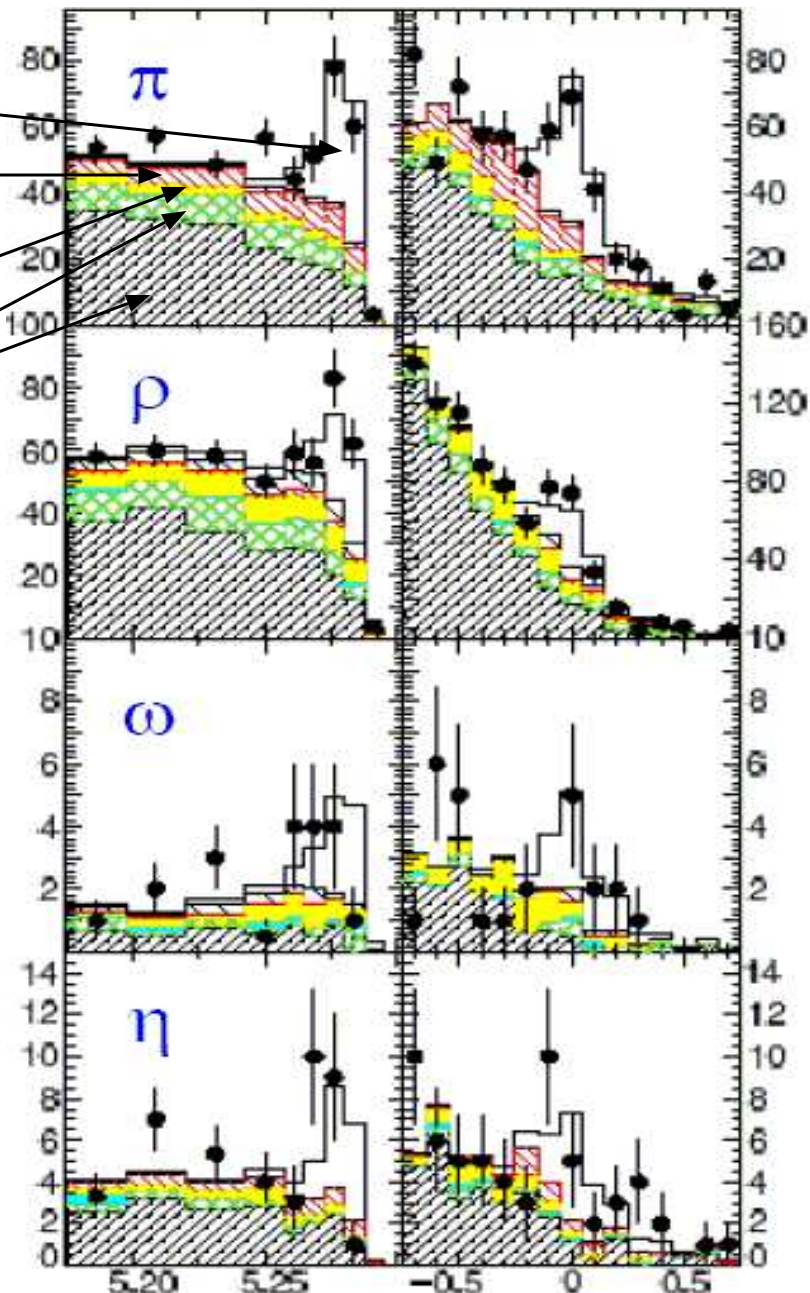
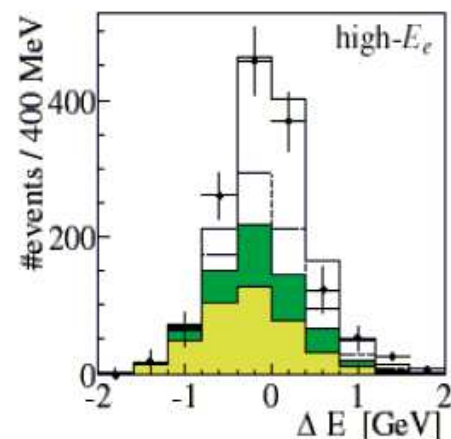
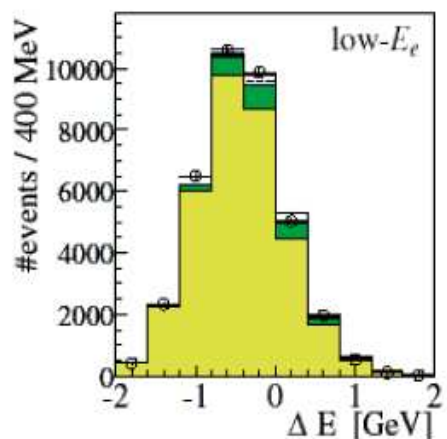
Measure ΔE , m_{bc} with neutrino reconstruction

CLEO 2003

$\rho l\nu$ Babar 2003



signal
crossfeed
downfeed
continuum
 $b \rightarrow cl\nu$



CLEO $\pi l\nu + \rho l\nu$:

$$|V_{ub}| = (3.17 \pm 0.17_{-0.17}^{+0.16+0.53}) \times 10^{-3}$$

BaBar $\rho l\nu$:

$$|V_{ub}| = (3.64 \pm 0.22 \pm 0.25_{-0.56}^{+0.39}) \times 10^{-3}$$

[Vub] inclusive analysis: Introduction

Inclusive Xulu measurement:

→ suffer from large Xc Inu background

→ measure the rate in limited kinematical region

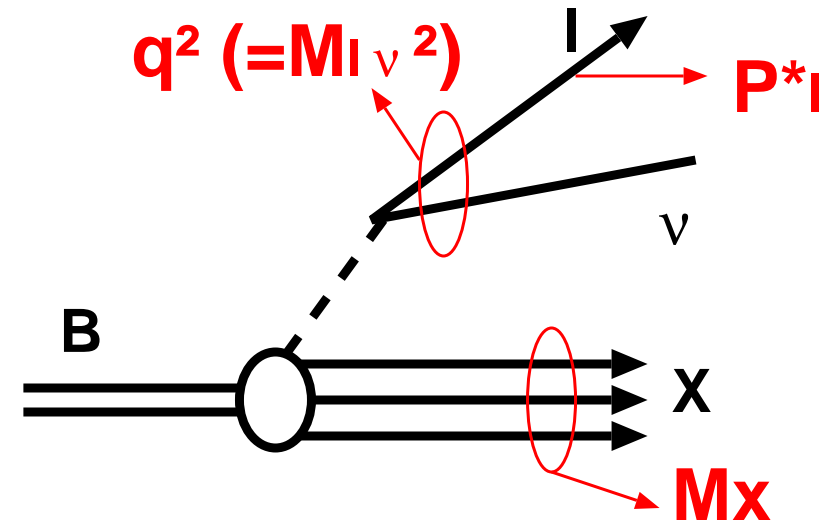
Use three kinematical variables:

	P^*_l	M_x	q^2
experimental accessibility	✓	X	X
frac. beyond Xclv limit	10%	70%	20%

Two types of analysis

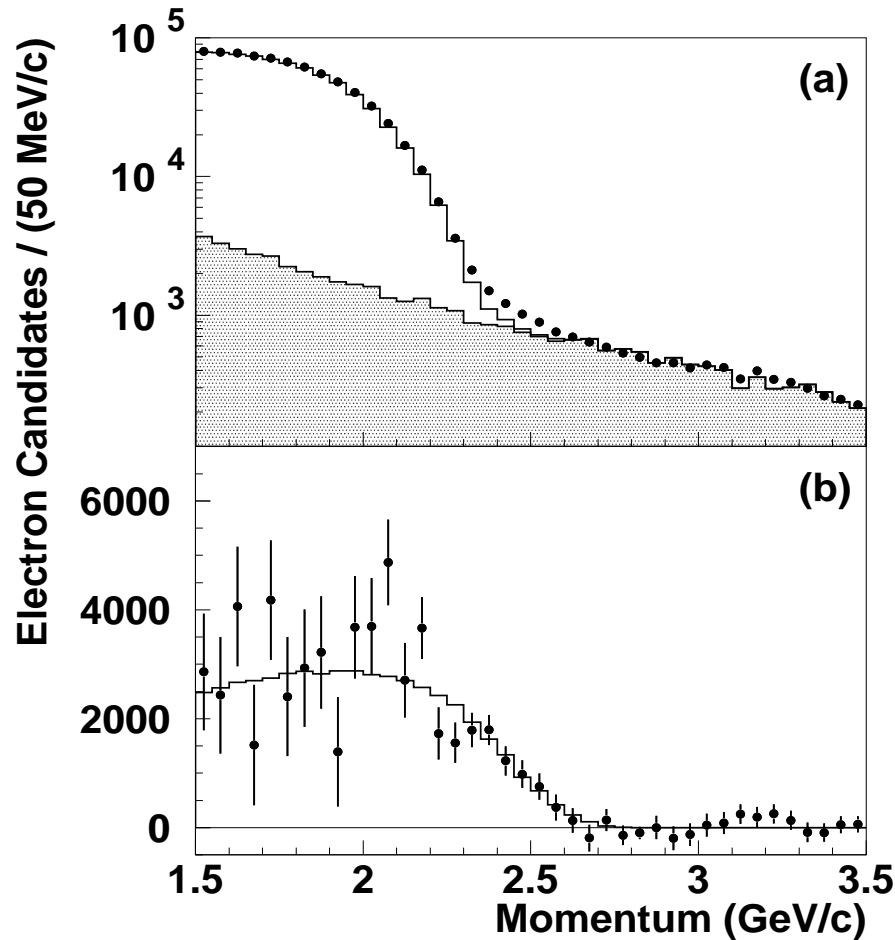
1. P^*_l endpoint analysis

2. M_x , q^2 measurement



$|V_{ub}|$ inclusive analysis: p^*_l endpoint analysis

p^*_l spectrum Belle 29/fb preliminary



Measure partial Br. around lepton momentum endpoint:

$$\Delta\text{Br}(B \rightarrow Xu\nu; 2.3 < p_e < 2.6 \text{ GeV}) = (1.18 \pm 0.11 \pm 0.10) 10^{-4}$$

Extrapolation factor w/
CLEO's $b \rightarrow s\gamma$ measurement
← reduce the theoretical uncertainty

$$f_u(\Delta p) = 0.130 \pm 0.024 \pm 0.015$$

$$\text{Br}(B \rightarrow Xu\nu) = \Delta\text{Br} / f_u(\Delta p) = (1.60 \pm 0.15 \pm 0.14 \pm 0.44) 10^{-3}$$

$$|V_{ub}| = (3.96 \pm 0.18 \pm 0.17 \pm 0.55 \pm 0.22) \times 10^{-3}$$

stat
syst
fu
 $\Gamma \rightarrow V_{ub}$

|Vub| inclusive analysis: M_x, q^2 measurement

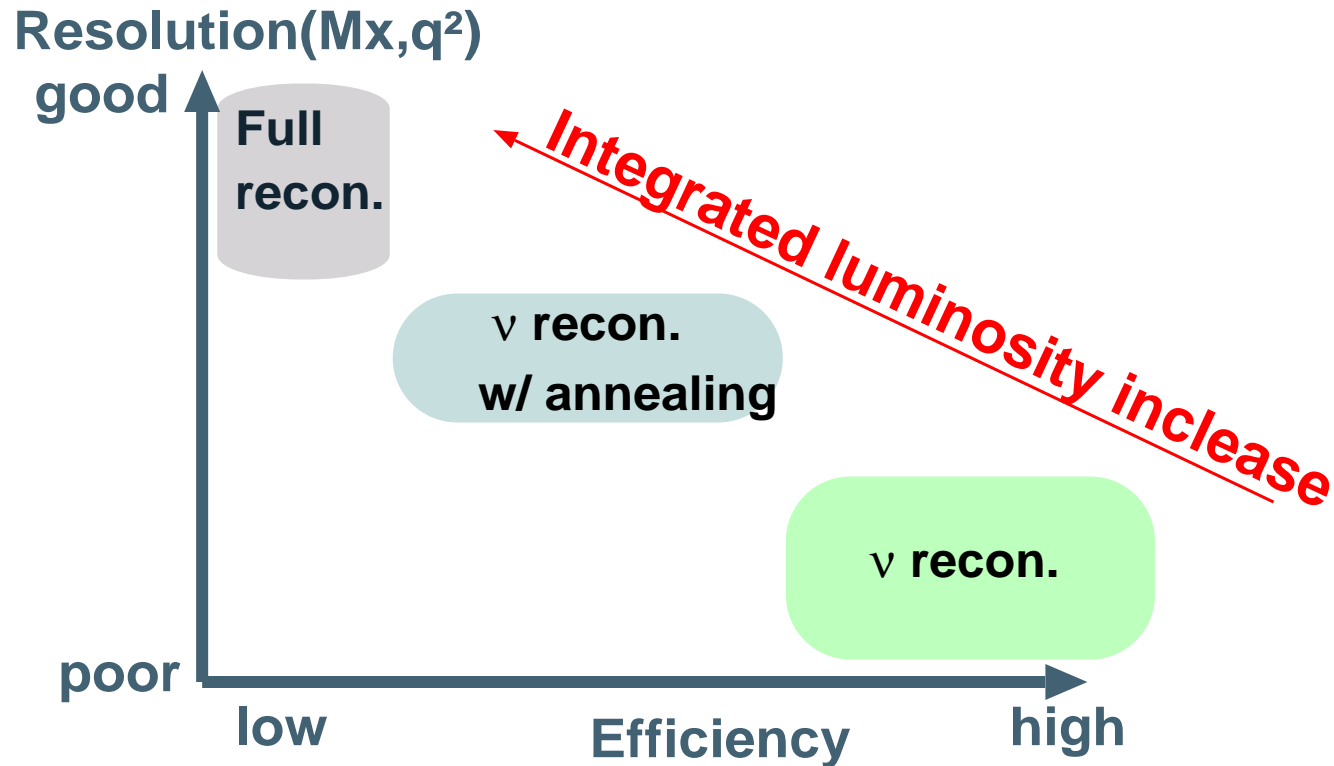
Measuring M_x : good separation from $X_{cl\nu}$ can be achieved

Using M_x & q^2 cuts: theoretical uncertainty can be much reduced

← avoid the region where the OPE breaks down

M_x, q^2 measurements:

have different strategies according to the amount of Luminosity



$|V_{ub}|$ inclusive analysis: M_X, q^2 from neutrino recon.

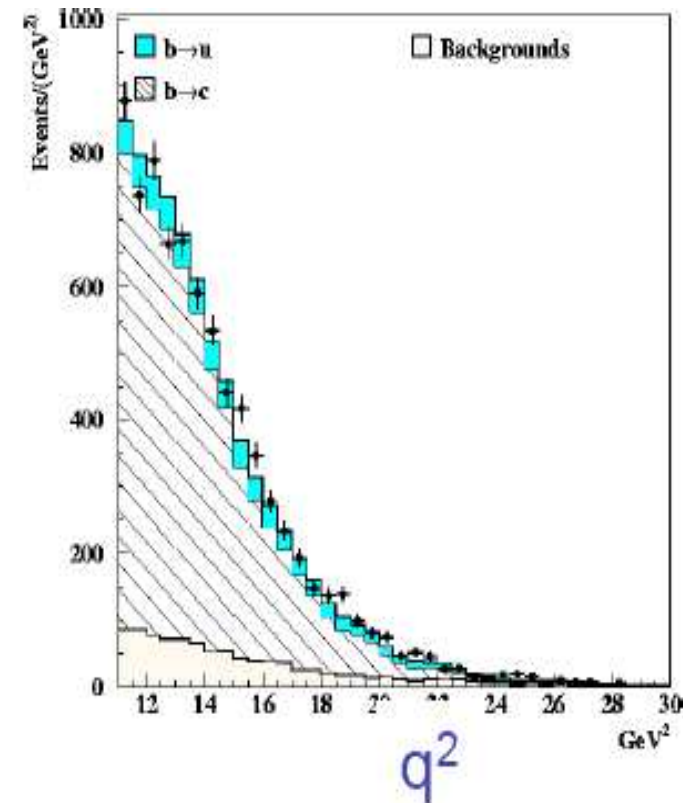
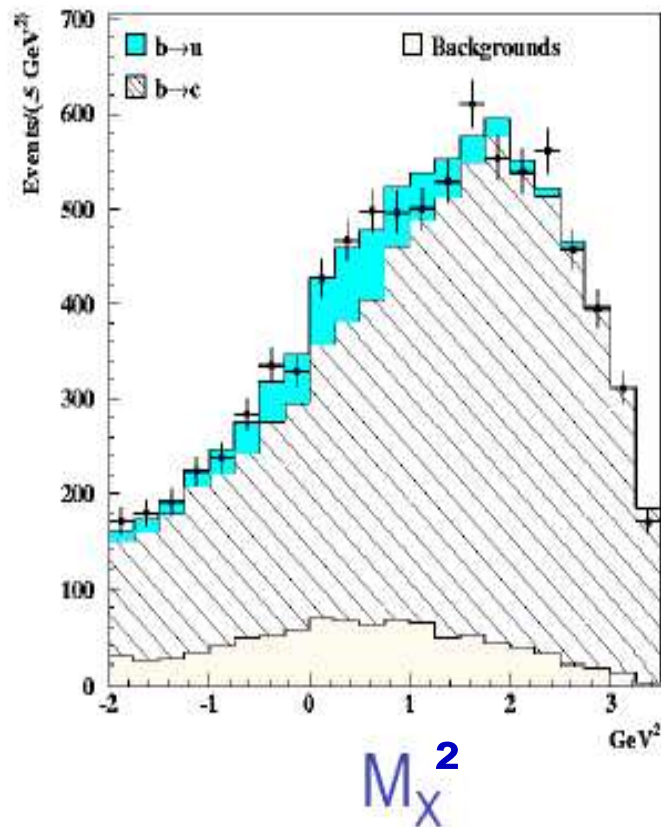
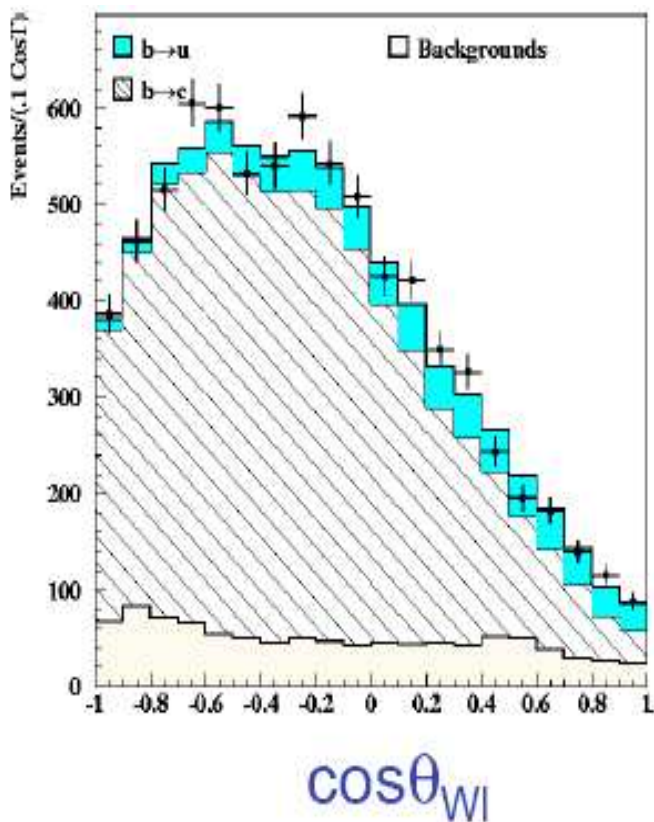
CLEO 9.4/fb preliminary

Neutrino reconstruction:

$$\mathbf{p}_\nu = \mathbf{p}_{\text{beam}} - \mathbf{p}_{\text{vis.}}, \quad E_\nu = E_{\text{beam}} - E_{\text{vis.}} \quad \Delta p_\nu \sim 120 \text{ MeV}$$

$$\rightarrow q^2 = (E_l + E_\nu)^2 - |\mathbf{p}_l + \mathbf{p}_\nu|^2$$

$$M_X^2 \sim M_B^2 + q^2 - 2 E_{\text{beam}} (E_l + E_\nu) + 2 |\mathbf{p}_b| |\mathbf{p}_l| \cos \theta_{B,l\nu}$$



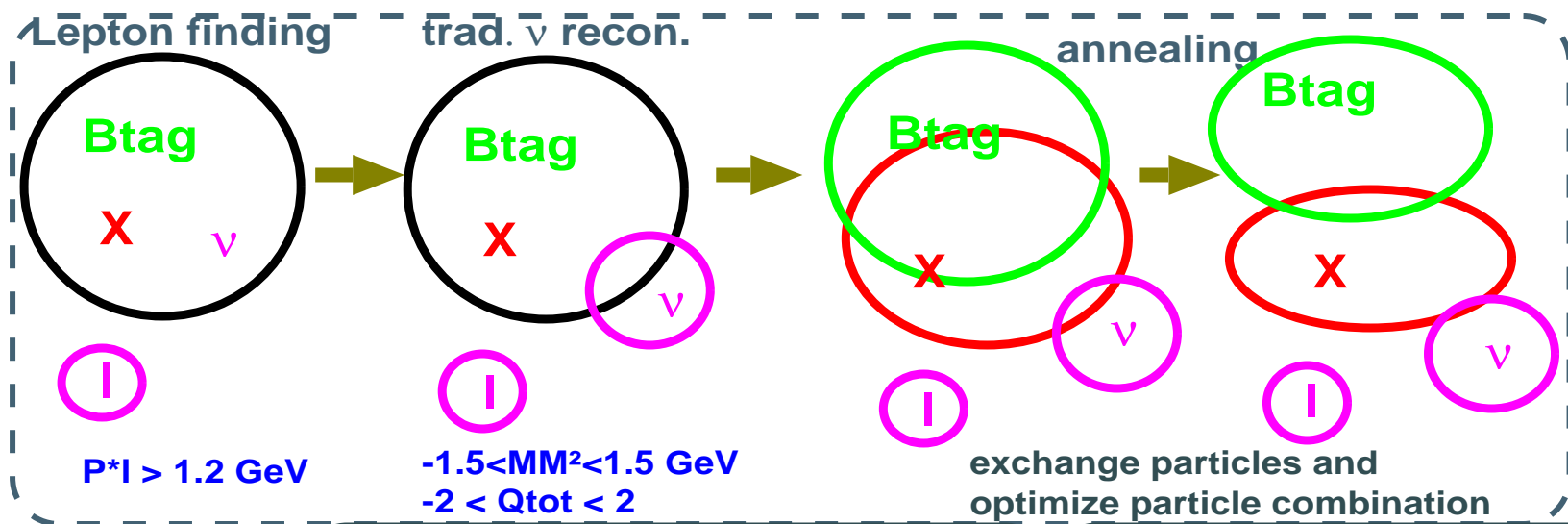
Use: $q^2 > 11 \text{ GeV}^2$, $M_X < 1.5 \text{ GeV}$

$$|V_{ub}| = (4.05 \pm 0.18 \pm 0.58 \pm 0.25 \pm 0.21 \pm 0.56) \times 10^{-3}$$

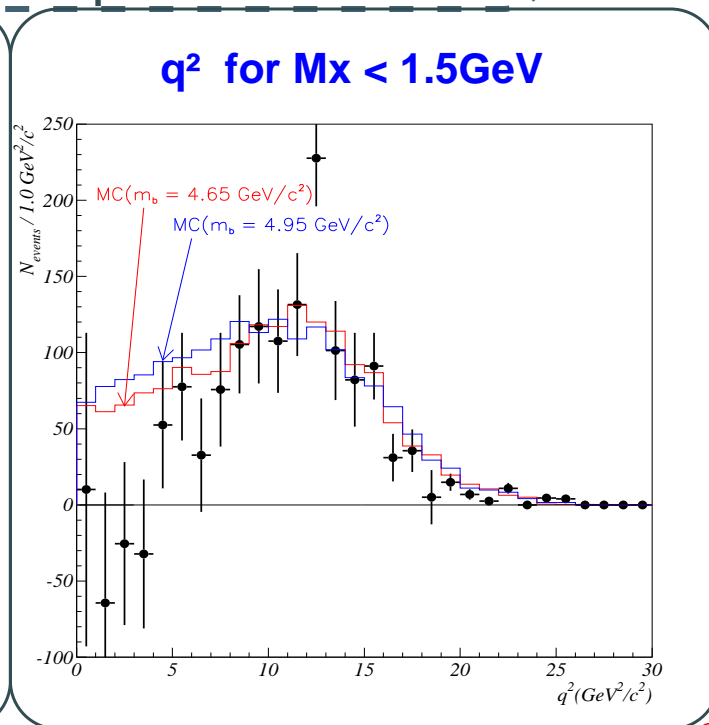
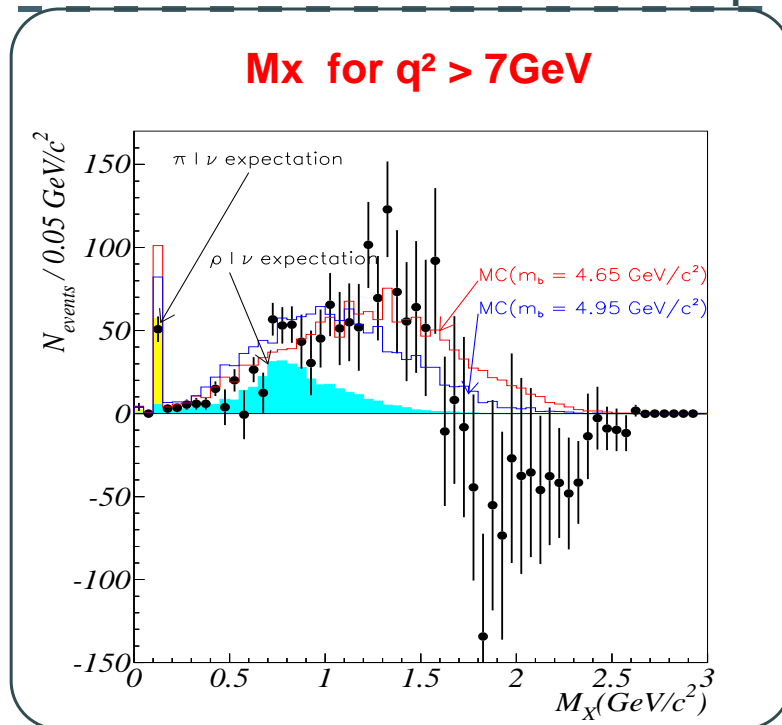
stat
syst
b→c
b→u
theory

$|V_{ub}|$ inclusive analysis: M_X, q^2 from ν recon. w/ annealing

Belle 78/fb preliminary



Combined cuts
on M_X & q^2 :
 $M_X < 1.5 \text{ GeV}$
 $q^2 > 7 \text{ GeV}^2$



$$|V_{ub}| = (3.96 \pm 0.17 \pm 0.44 \pm 0.34 \pm 0.26 \pm 0.29) \times 10^{-3}$$

stat syst $b \rightarrow c$ shape $\Gamma \rightarrow |V_{ub}|$

$|V_{ub}|$ inclusive analysis: M_X from full recon.

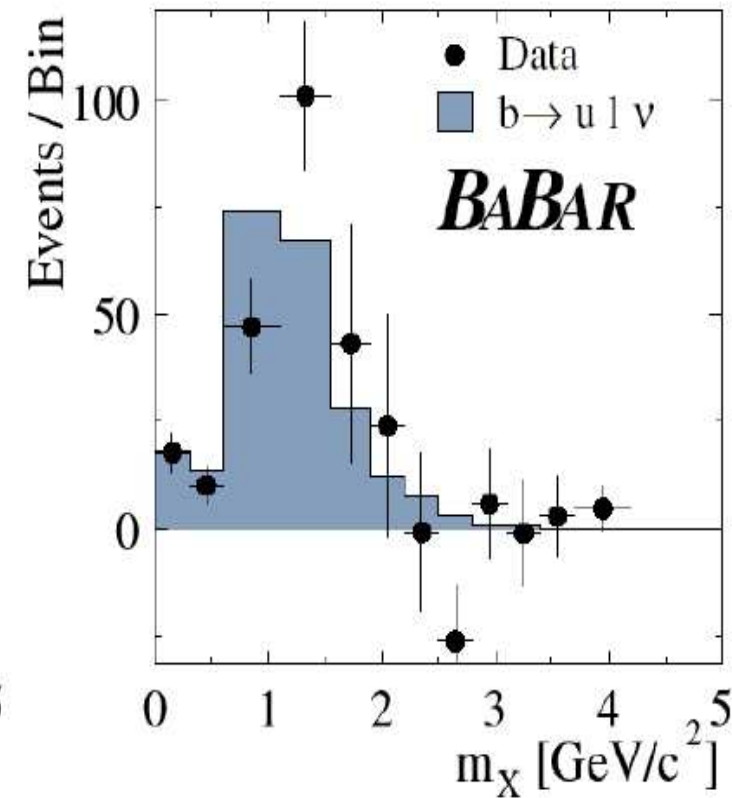
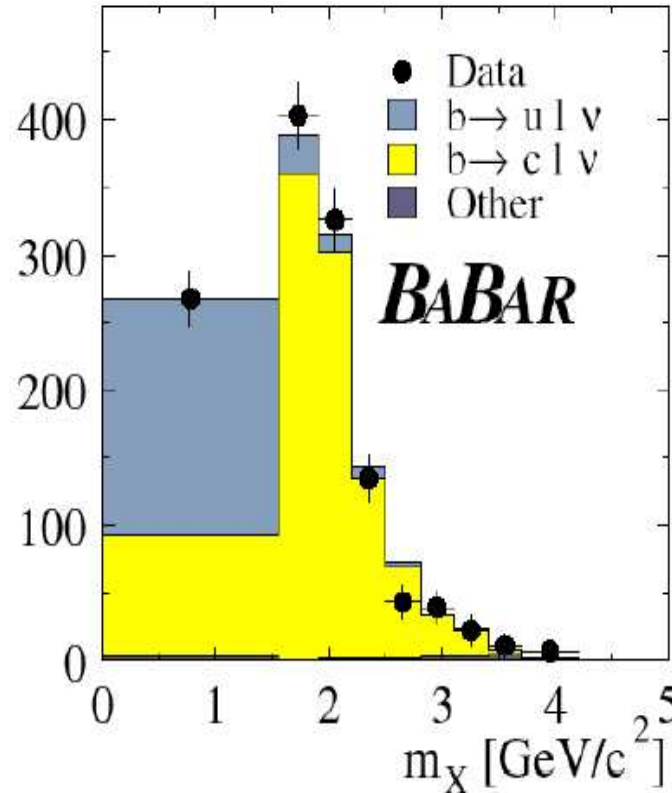
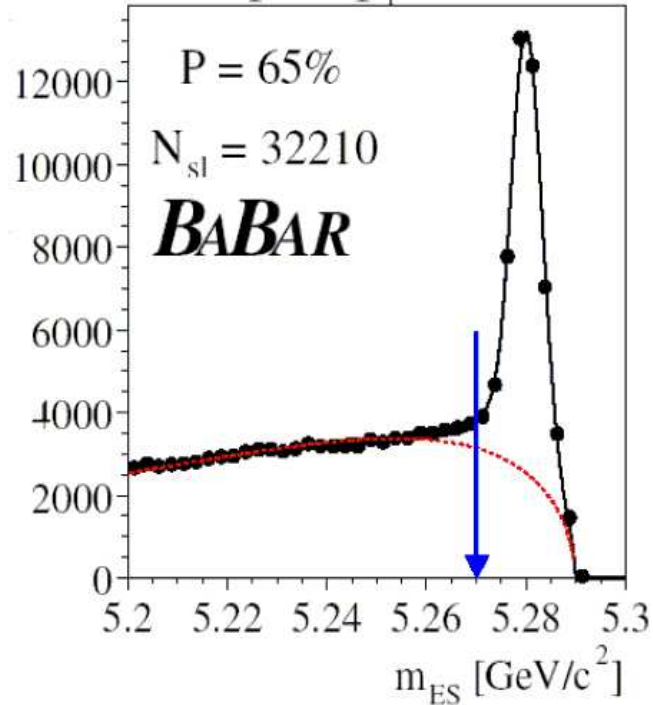
Babar 89M $\Upsilon(4S)$

$\Upsilon(4S) \rightarrow B_{\text{reco}} B_{\text{sig}}$

Fully reconstruct

Reconstruct M_X in $Xl\nu$

1 lepton, $p_l > 1 \text{ GeV}/c$



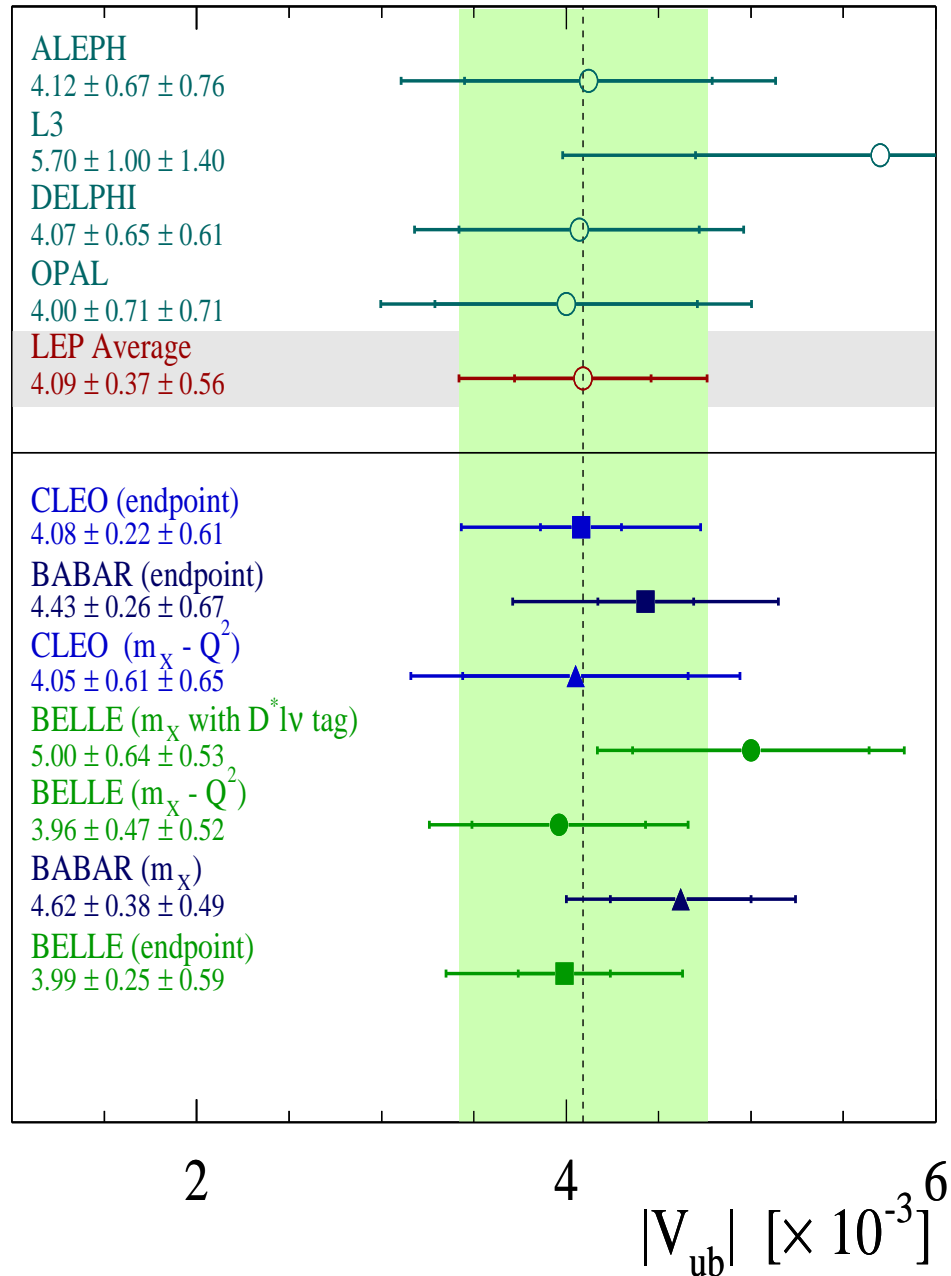
Use $M_X < 1.55 \text{ GeV}$ region

With $\bar{\Lambda} = 0.48 \pm 0.12 \text{ GeV}$, $\lambda_1 = -0.30 \pm 0.11 \text{ GeV}$:

$$|V_{ub}| = (4.62 \pm 0.28 \pm 0.27 \pm 0.40 \pm 0.26) \times 10^{-3}$$

stat
syst
shape
 $\Gamma \rightarrow V_{ub}$

$|V_{ub}|$ inclusive measurements summary



What about averaged value of $|V_{ub}|$?

Evaluation of uncertainty with same theory error is necessary



Updated Belle's ν recon with annealing with same $\bar{\Lambda}$ error as BaBar

→ go out soon

Summary

- Extensive studies for $|V_{cb}|$, $|V_{ub}|$ measurements are carrying on

$|V_{cb}|$ & $|V_{ub}|$ values:

- theoretical uncertainty limit its precision
- moment analyses are of great importance for reducing the theoretical uncertainty

Belle & BaBar are accumulating $> 100/\text{fb}$

Large number of fully reconstructed B samples are available

- much reduce the experimental systematics of various inclusive analyses

→ $|V_{ub}|$, $|V_{cb}|$ are kept updating to be a good constraint on the unitarity triangle

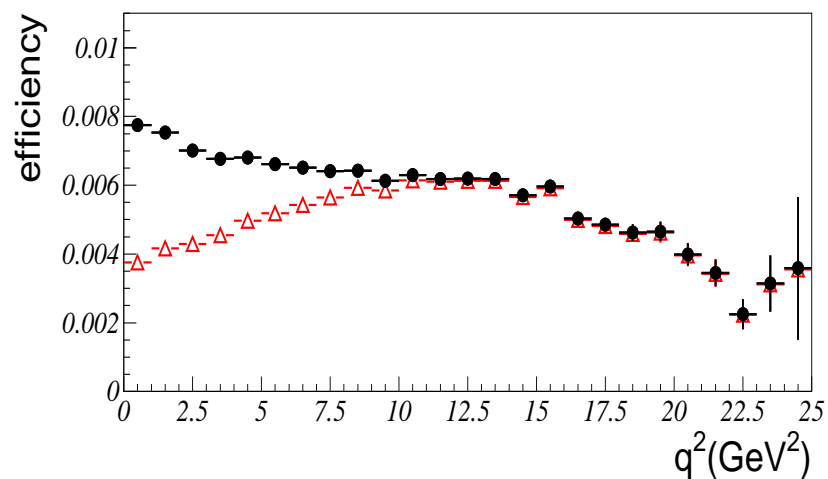
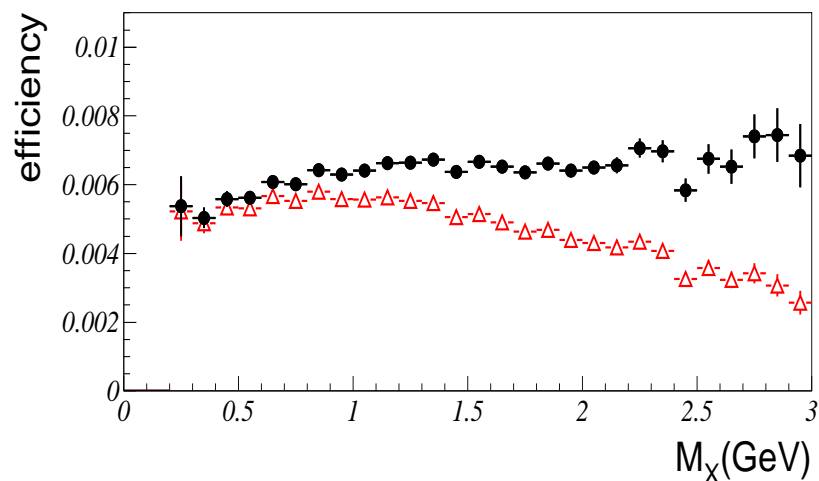
- $|V_{ub}|$ averaging among the various measurements are needed!
Belle will provide updated results of ν recon. with annealing with $\Delta m_b = 0.12 \text{ GeV}$ (compatible to BaBar's)
→ first step for the $|V_{ub}|$ averaging

More details of $|V_{cb}|$, $|V_{ub}|$, moment analyses will be discussed at morning sessions on Thursday

Backup slides

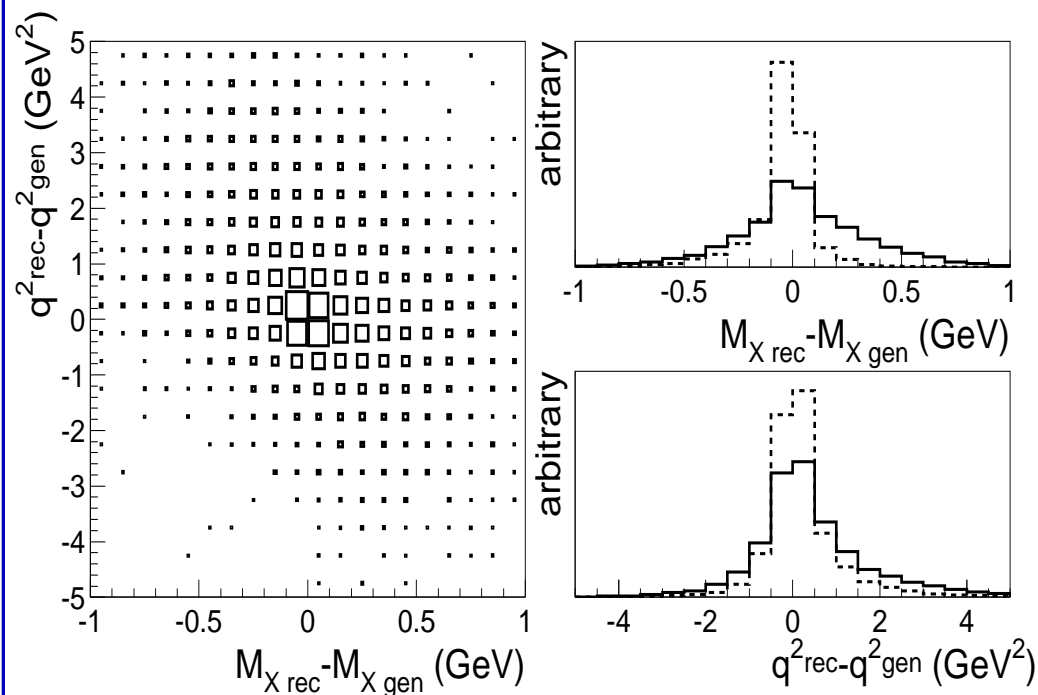
Qualities of reconstruction

Mx, q² dependence of efficiency



closed circle: efficiency against $P^*|>1.2\text{GeV}$
open triangle: efficiency against the whole events

Mx and q² resolution



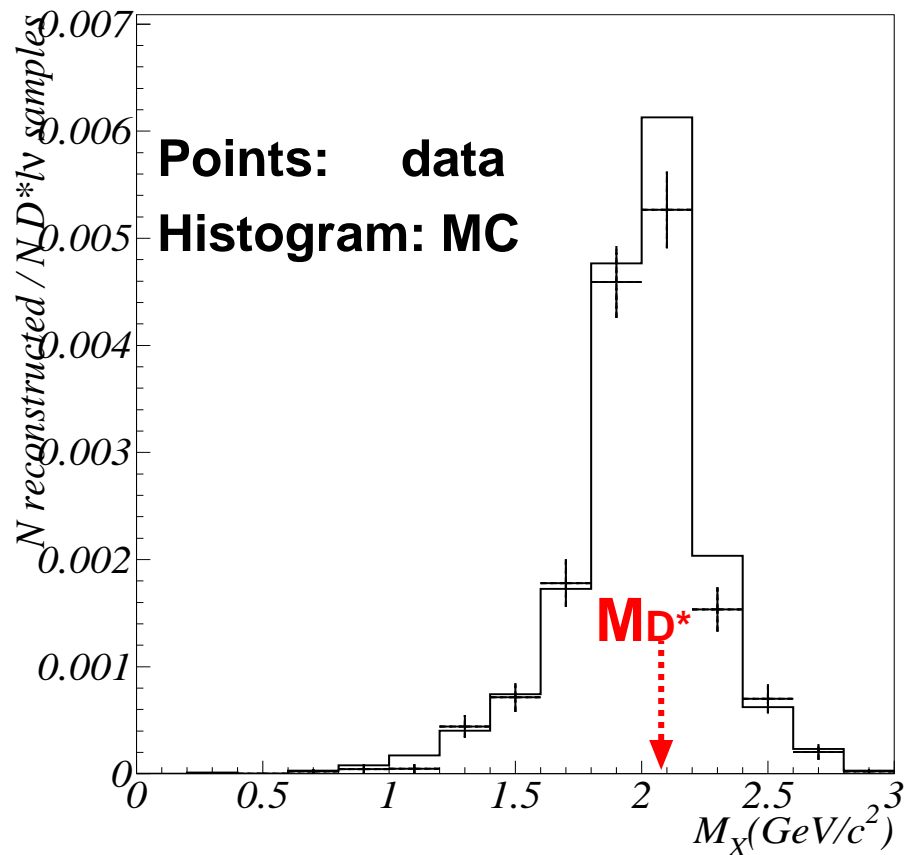
dashed histogram : resolutions by perfect identification of X_u and B_{tag}
closed histo.& 2dim. hist.: resolutions by annealing

|Vub| inclusive analysis: Neutrino reconstruction w/ annealing

control samples

B → D*lv samples

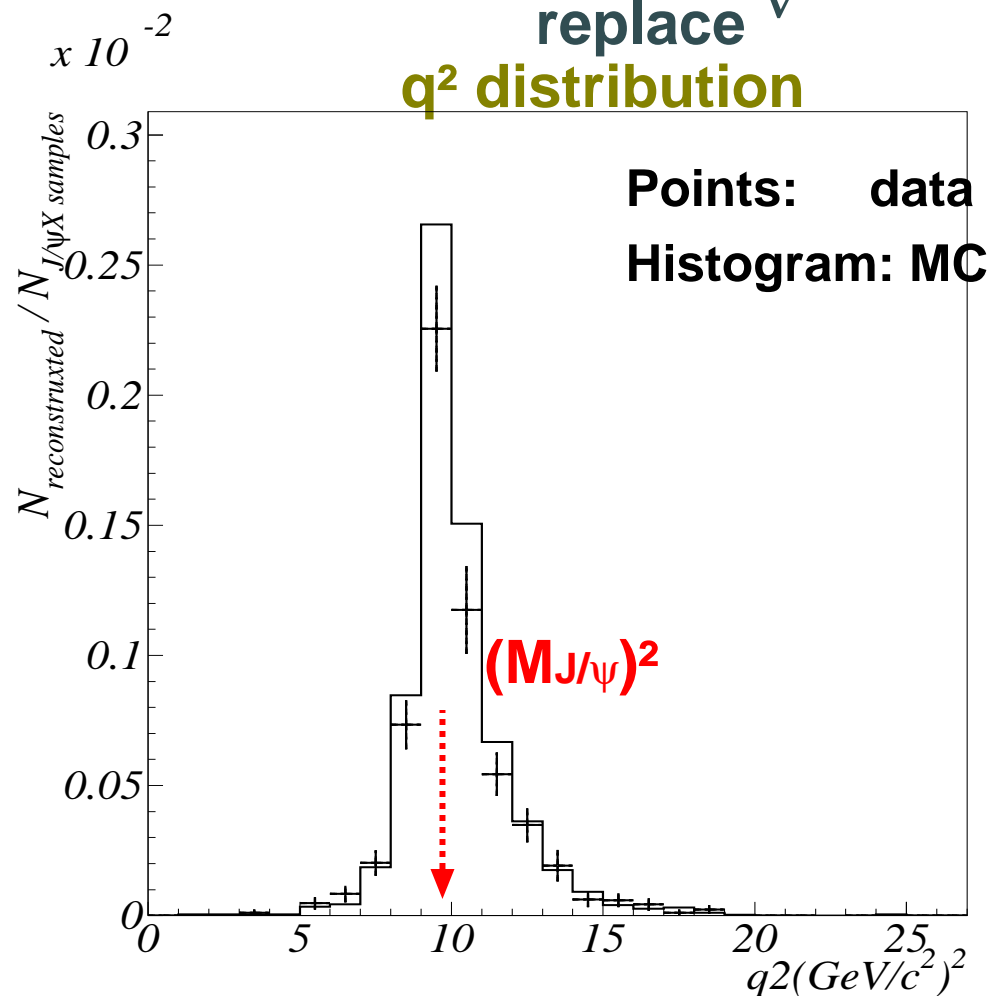
Mx distribution



	mean (GeV/c ²)	RMS(GeV/c ²)
data	1.98	0.29
MC	1.99	0.30

B → J/ψ(J/ψ → ll) X samples

replace \vec{v} q² distribution

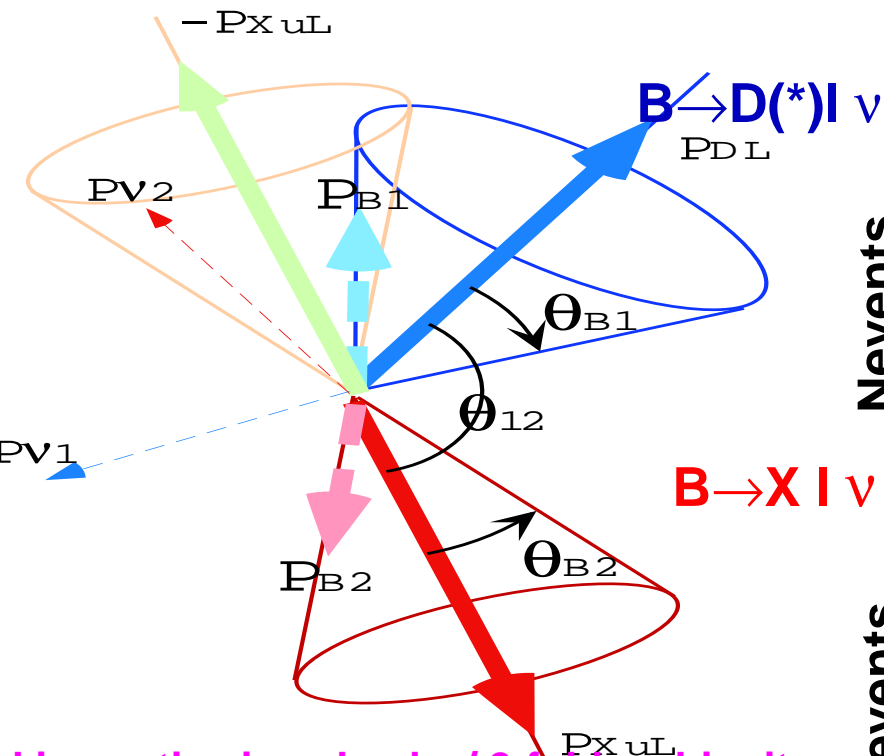


	mean (GeV ² /c ²)	RMS(GeV ² /c ²)
data	10.2	1.9
MC	10.2	1.8

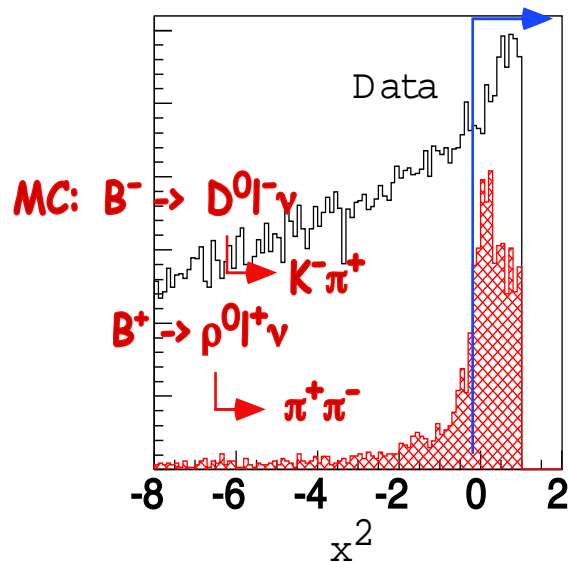
$|V_{ub}|$ inclusive analysis: M_X from D^* $l \nu$ tag

Belle 78/fb preliminary

Direction of B-mesons

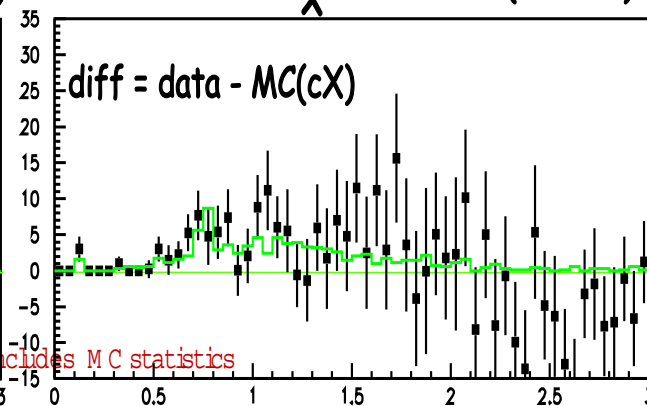
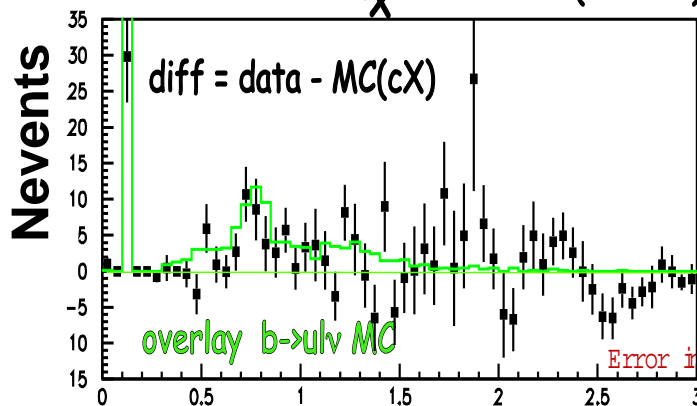
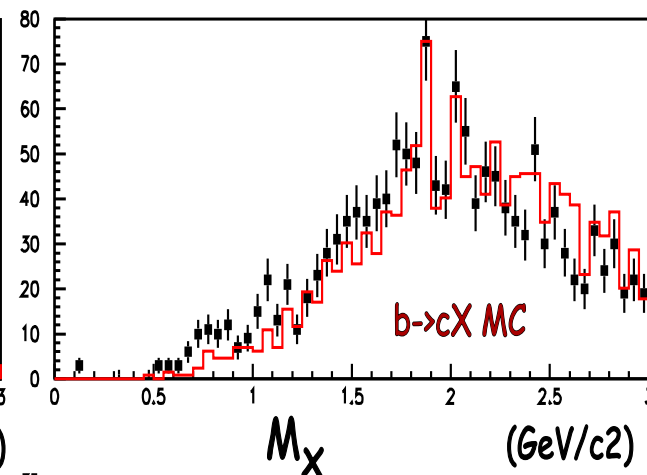
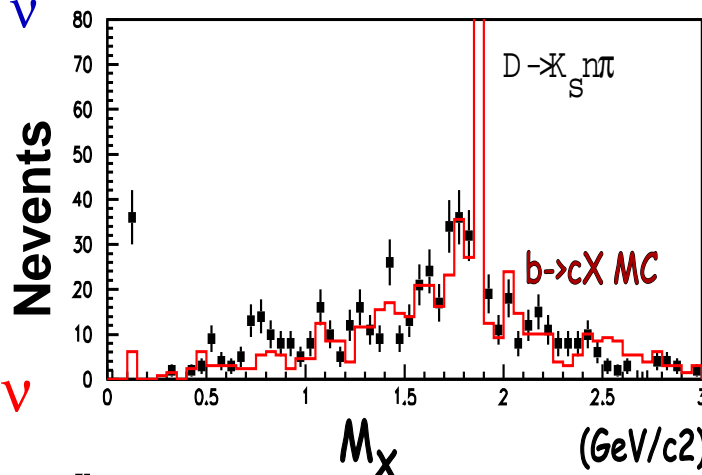


kinematics is solved w/ 2-fold ambiguity



all-charged mode

π^0 -assoc. mode



82 ± 19 events in $M_X < 1.5$ GeV

92 ± 21 events in $M_X < 1.5$ GeV

$$|V_{ub}| = (5.00 \pm 0.60 \pm 0.23 \pm 0.05 \pm 0.39 \pm 0.36) \times 10^{-3}$$

stat syst $b \rightarrow c$ $b \rightarrow u$ theory